

The Constructive Semantics

- Logical correctness is not in accordance with the intention of the language, ie with its intuitive semantics and with the intended sequential character of test statements.
- Example:

```
module P10:  
  present O then nothing end; emit O
```

is logically correct, but the information that O is present flows backwards across the sequencing operator ; contradicting the basic intuition about sequential execution.

- Aside from the explicit concurrency || all Esterel statements are sequential.

The Constructive Semantics

- Idea: do not check assumptions about signal statuses, but propagate facts about control flow and signal statuses. Self-justification is replaced by fact-to-fact propagation.
- Accounts for programmer's natural way of thinking: in terms of cause and effect.
- Three-valued logic for signals: present, absent, unknown.
- In each instant the statuses of the input signals are given by the environment and the statuses of the other signals are initially set to unknown.

The Constructive Semantics

- Three equivalent presentations:
 - Constructive behavioral semantics
 - Derived from the logical behavioral semantics
 - Constructive restrictions are added to the logical coherence rule
 - Constructive operational semantics
 - Based on term rewriting rules defining microstep sequences
 - Simplest way of defining an efficient interpreter
 - Circuit semantics
 - Translation of program into constructive circuits
 - Core of the Esterel v5 compiler.

Constructive Behavioral Semantics

- Logical coherence semantics augmented by reasoning about what a program **must** or **cannot** do, both predicates being disjoint and defined in a constructive way.
- The **must** predicate determines which signals are present and which statements are executed.
- The **cannot** predicate determines when signals are absent and it serves in pruning out false execution paths.
- A program is accepted as **constructive** if and only if fact propagation using the **must** and **cannot** predicates suffices in establishing presence or absence of all signals.

Constructive Behavioral Semantics

- Logical Coherence Law:
 - A signal S is present in an instant iff an `emit S` statement is executed in this instant.
- Constructive Coherence Law:
 - A signal S is present iff an `emit S` statement must be executed.
 - A signal S is absent iff an `emit S` statement cannot be executed.

Constructive Behavioral Semantics

- A signal can have three statuses:
 - $+$: known to be present
 - $-$: known to be absent
 - \perp : yet unknown
- must and cannot predicates are defined by structural induction on statements.
- $p ; q$
 - Must (resp. can) execute q if p must (resp. can) terminate
- present S then p else q end
 - S known to be present \rightarrow Test behaves as p
 - S known to be absent \rightarrow Test behaves as q
 - S yet unknown \rightarrow Test can do whatever p or q can do; there is nothing the test must do.

Example 1

```
module P1:
input I;
output O;
signal S1, S2 in
  present I then emit S1 end (i1)
  ||
  present S1 else emit S2 end (i2)
  ||
  present S2 then emit O end (i3)
end signal
end module
```

- If I is present:
 - i1 must take its **then** branch, **emit S1** and terminate → S1 present
 - i2 must take its (empty) **then** branch and cannot take its **else** branch → **emit S2** cannot be executed, S2 cannot be emitted → S2 absent
 - i3 cannot take its **then** branch → O cannot be emitted and is absent.
- If I is absent:
 - i1 cannot take its **then** branch → **emit S1** cannot be executed → S1 absent
 - i2 must take its **then** branch → **emit S2** must be executed → S2 present.
 - i3 must take its **then** branch → **emit O** must be executed → O present.

Example 2 – Part 1

```
module P2:
  output O;
  signal S in
    emit S;
    present O then
      present S then
        pause
      end;
      emit O
    end
  end signal
```

- Analyze what **signal S** must do with status \perp for O.
 - Analyze body with status \perp for O and S.
 - S must be emitted.
 - Thus: redo the analysis with status \perp for O and + for S.
 - Status of O is unknown: there is nothing that the **present** statement **must** do. Progress can only be made by analyzing what we **cannot** do in the branches of the test.
 - The *then* branch contains a **present S** test. Since S is known to be present, we **cannot** take the implicit *else* branch. Since the *then* branch is a **pause** statement it **cannot** terminate. Therefore the **emit O** statement **cannot** be executed and O **cannot** be emitted.
 - As a consequence O **must** be set absent and the analysis **must** be redone with status – for O.

Example 2 – Part 2

```
module P2:
output 0;
signal S in
emit S;
present 0 then
present S then
pause
end;
emit 0
end
end signal
```

- Analyze what **signal S** must do with status – for 0.
 - The implicit else branch of the present 0 test that terminates execution must be taken.
 - The program is **constructive** since we have fully determined the signal statuses.

Constructive Behavioral Semantics

- signal S in p end
 - Can: recursively analyze p with status \perp for S
 - Must:
 - Assume we already know that we must execute the declaration in some signal context E
 - Must compute final status of S to determine signal context of p
 - First analyze p in E augmented by setting the unknown status \perp for S
 - If S must be emitted:
 - propagate this information by reanalyzing p in E with S present
 - This may generate more information about the other signals
 - If S cannot be emitted:
 - reanalyze p in E with S absent

Constructive Behavioral Semantics – Formal Definition

- Let S be a set of signals.

An event E is a mapping $E : S \rightarrow B_{\perp} = \{+, -, \perp\}$ which assigns a status from B_{\perp} to all signals in S .

- Notation:

- $s^+ : E(s) = +$

- $s^- : E(s) = -$

- $E \subseteq E' : s^+ \text{ in } E \Rightarrow s^+ \text{ in } E'$

- Singleton event $\{s^+\}$:

$$\{s^+\}(s) = + \text{ and } \{s^+\}(s') = - \text{ for all } s' \neq s$$

- Let an event E for a set S be given, a signal s possibly not in S and a status b in B_{\perp} . Then $E * s^b$ is an event for the set $S \cup \{s\}$ where

$$E * s^b(s) = b \text{ and } E * s^b(s') = E(s') \quad \forall s' \neq s.$$

Constructive Behavioral Semantics – Formal Definition

- The statements **nothing**, **pause** and **exit** are represented by completion codes $k \geq 0$:
 - **nothing** is encoded by 0
 - **pause** is encoded by 1
 - **exit** T is encoded by 2, if the directly enclosing trap declaration is that of T and $n + 2$ if n trap declarations have to be traversed before reaching that of T .
- To handle trap propagation we define two operators

$$\downarrow k = \begin{cases} 0, & \text{if } k = 0 \text{ or } k = 2 \\ 1, & \text{if } k = 1 \\ k - 1, & \text{if } k > 2 \end{cases}$$

$$\uparrow k = \begin{cases} k, & \text{if } k = 0 \text{ or } k = 2 \\ k + 1, & \text{if } k > 1 \end{cases}$$

Constructive Behavioral Semantics – Formal Definition

- Given a program P with body p and an input event I . A reaction of the program is given by a behavioral transition of the form

$$P \xrightarrow[I]{O} P'$$

where O is an output event and the resulting program P' is the new state reached by P after the reaction. P' is called the derivative of P by the reaction.

- The statement transition relation has the form

$$p \xrightarrow[E]{E',k} p'$$

where

- E is an event that defines the status of all signals in the scope of p
- E' is an event composed of all signals emitted by p in the reaction, k is the completion code returned.

The statement p' is called the derivative of p by the reaction.

Constructive Behavioral Semantics – Formal Definition

$$P \xrightarrow[l]{o} P' \iff p \xrightarrow[l \cup o]{o, k} p' \text{ for some } k$$

$$\text{Max}(K, L) = \begin{cases} \emptyset & \text{if } K = \emptyset \text{ or } L = \emptyset \\ \{\max\{k, l\}\}, & \text{for } k \in K, l \in L \end{cases}$$

Constructive Behavioral Semantics – Formal Definition

- The `Must` function determines what must be done in a reaction

$$P \xrightarrow[i]{o} P'$$

$$\text{Must}(p, E) = \langle S, K \rangle$$

where

- E is an event,
 - S is the set of signals that p must emit
 - K is the set of completion codes that p must return.
- We write
 $\text{Must}(p, E) = \langle S, K \rangle =: \langle \text{Must}_s(p, E), \text{Must}_k(p, E) \rangle$.

Constructive Behavioral Semantics – Formal Definition

- The function $\text{Cannot}^m(p, E)$ is used to prune out false paths.

$$\text{Cannot}^m(p, E) = \langle \text{Cannot}_s^m(p, E), \text{Cannot}_k^m(p, E) \rangle = \langle S, K \rangle$$

- S is the set of signals that p cannot emit
 - K is the set of completion codes that p cannot exit with when the input event is E .
-
- $m \in \{+, \perp\}$ indicates whether it is known that the statement p must be executed in the event E . The case $m = -$ will never occur since Cannot will only be called for potentially executable statements.
-
- In the following, we will use $\text{Can}^m(p, E)$ since it is easier to be defined formally; from this, $\text{Cannot}^m(p, E)$ can be determined by componentwise complementation.

Constructive Behavioral Semantics – Formal Definition

- *Must* and *Can^m* are defined by structural induction over the kernel statements.

$$\mathit{Must}(k, E) = \mathit{Can}^m(k, E) = \langle \emptyset, \{k\} \rangle$$

$$\mathit{Must}(\mathit{emit } S, E) = \mathit{Can}^m(\mathit{emit } S, E) = \langle \{s\}, \{0\} \rangle$$

$$\mathit{Must}(\mathit{present } s \text{ then } p \text{ else } q \text{ end}, E) = \begin{cases} \mathit{Must}(p, E), & \text{if } s^+ \in E \\ \mathit{Must}(q, E), & \text{if } s^- \in E \\ \langle \emptyset, \emptyset \rangle, & \text{if } s^\perp \in E \end{cases}$$

$$\mathit{Can}^m(\mathit{present } s \text{ then } p \text{ else } q \text{ end}, E) = \begin{cases} \mathit{Can}^m(p, E), & \text{if } s^+ \in E \\ \mathit{Can}^m(q, E), & \text{if } s^- \in E \\ \mathit{Can}^\perp(p, E) \cup \mathit{Can}^\perp(q, E), & \text{if } s^\perp \in E \end{cases}$$

$$\mathit{Must}(\mathit{suspend } p \text{ when } s, E) = \mathit{Must}(p, E)$$

$$\mathit{Can}^m(\mathit{suspend } p \text{ when } s, E) = \mathit{Can}^m(p, E)$$

Constructive Behavioral Semantics – Formal Definition

$$Must(p; q, E) = \begin{cases} Must(p, E), & \text{if } Must_k(p, E) \neq \{0\} \\ \langle Must_s(p, E) \cup Must_s(q, E), Must_k(q, E) \rangle, & \text{if } Must_k(p, E) = \{0\} \end{cases}$$

We analyze q only if p must terminate in which case the completion code 0 of p is discarded.

Constructive Behavioral Semantics – Formal Definition

$$\text{Can}^m(p; q, E) = \left\{ \begin{array}{l} \text{Can}^m(p, E), \\ \qquad \qquad \qquad \text{if } 0 \notin \text{Can}_k^m(p, E) \\ \left\langle \text{Can}_s^m(p, E) \cup \text{Can}_s^{m'}(q, E), \text{Can}_k^m(p, E) \setminus \{0\} \cup \text{Can}_k^{m'}(q, E) \right\rangle \\ \qquad \qquad \qquad \text{if } 0 \in \text{Can}_k^m(p, E) \text{ with } m' = + \text{ if } m = + \\ \qquad \qquad \qquad \text{and } 0 \in \text{Must}_k(p, E) \\ \qquad \qquad \qquad \text{or if } 0 \in \text{Can}_k^m(p, E) \text{ with } m' = \perp \text{ otherwise} \end{array} \right.$$

We analyze q with argument $m' = +$ if $m = +$ and if p must terminate, with argument $m' = \perp$ otherwise.

Constructive Behavioral Semantics – Formal Definition

$$\text{Must}(\text{loop } p \text{ end}, E) = \text{Must}(p, E)$$

$$\text{Can}^m(\text{loop } p \text{ end}, E) = \text{Can}^m(p, E)$$

$$\text{Must}(p \parallel q, E) = \left\langle \text{Must}_s(p, E) \cup \text{Must}_s(q, E), \text{Max}(\text{Must}_k(p, E), \text{Must}_k(q, E)) \right\rangle$$

$$\text{Can}^m(p \parallel q, E) = \left\langle \text{Can}_s^m(p, E) \cup \text{Can}_s^m(q, E), \text{Max}(\text{Can}_k^m(p, E), \text{Can}_k^m(q, E)) \right\rangle$$

- The Max operation e.g. ensures that \parallel cannot terminate if one of its branches cannot do so.

Constructive Behavioral Semantics – Formal Definition

$$\text{Must}(\text{trap } T \text{ in } p \text{ end}, E) = \text{Must}(\{\uparrow p\})$$

$$\text{Must}(\{q\}, E) = \langle \text{Must}_s(q, E), \downarrow \text{Must}_k(q, E) \rangle$$

$$\text{Must}(\uparrow q, E) = \langle \text{Must}_s(q, E), \uparrow \text{Must}_k(q, E) \rangle$$

$$\text{Can}^m(\text{trap } T \text{ in } p \text{ end}, E) = \text{Can}^m(\{\uparrow p\})$$

$$\text{Can}^m(\{q\}, E) = \langle \text{Can}_s^m(q, E), \downarrow \text{Can}_k^m(q, E) \rangle$$

$$\text{Can}^m(\uparrow q, E) = \langle \text{Can}_s^m(q, E), \uparrow \text{Can}_k^m(q, E) \rangle$$

Constructive Behavioral Semantics – Formal Definition

$$\begin{aligned}
 \text{Must}(\text{signal } s \text{ in } p, E) &= \begin{cases} \text{Must}(p, E * s^+) \setminus \{s\}, & \text{if } s \in \text{Must}_s(p, E * s^\perp) \\ \text{Must}(p, E * s^-) \setminus \{s\}, & \text{if } s \notin \text{Can}_s^+(p, E * s^\perp) \\ \text{Must}(p, E * s^\perp) \setminus \{s\}, & \text{otherwise} \end{cases} \\
 \text{Can}^m(\text{signal } s \text{ in } p, E) &= \begin{cases} \text{Can}^+(p, E * s^+) \setminus \{s\}, & \text{if } m = + \text{ and } s \in \text{Must}_s(p, E * s^\perp) \\ \text{Can}^m(p, E * s^-) \setminus \{s\}, & \text{if } s \notin \text{Can}_s^+(p, E * s^\perp) \\ \text{Can}_s^m(p, E * s^\perp) \setminus \{s\}, & \text{otherwise} \end{cases}
 \end{aligned}$$

- We first analyze the body p with status \perp for s with the same m argument.
- If $m = +$ and we find that the signal must be emitted we reanalyze p with status $+$ for s .
- For both $m = +$ and $m = \perp$ if the signal cannot be emitted we reanalyze p with status $-$ and with the same m .
- Otherwise we return the result of the analysis of p with status \perp for s .
- Note that the signal status can be set to $+$ only if $m = +$. This is necessary to avoid speculative computations.

Constructive Behavioral Semantics

- The constructiveness analysis involves many recomputations: Once a signal status has been set, the body of its declaration (the whole program for an output) has to be reanalyzed, this way re-establishing many facts that are already known.
- The goal of the operational and circuit semantics is to avoid recomputing known facts.

Example

```
module P4:  
input I;  
output O;  
signal S1, S2 in  
  present I then emit S1 end  
  ||  
  present S1 then emit S2 end  
  ||  
  present S2 then emit O end  
end module
```

accepted by constructiveness

```
module P3:  
input I;  
output O1, O2;  
present I then  
  present O2 then emit O1 end  
else  
  present O1 then emit O2 end  
end present  
end module
```

rejected by acyclicity test
reactive and deterministic
accepted by constructiveness

Examples

```
module P1:  
output 0;  
  present 0  
    else emit 0  
  end present  
end module
```

rejected by constructiveness

```
module P2:  
output 0;  
  present 0  
    then emit 0  
  end present  
end module
```

rejected by constructiveness

Examples

```
module Px:  
output 0;  
  present 0 then emit 0 else emit 0  
end module
```

logically correct by self
justification
rejected by constructiveness

Advanced Constructiveness

- Preemption statements behave as tests for the guard in each instant where the guard is active. Their constructiveness test is straightforward.

```
module Py:  
output 0;  
abort  
  sustain 0  
when 0
```

non-constructive in the first instant
non-constructive (non reactive) in later instants

Advanced Constructiveness

- Preemption statements (`abort`) behave as tests for the guard in each instant where the guard is active. Their constructiveness test is straightforward.
- Signal expressions:
 - `not e`: straightforward
 - `e1 or e2`: evaluates to true as soon as one of `e1` or `e2` evaluates to true, even if the other one is still unknown.
 - `e1 and e2`: analogous
- The computation of values of `valued signals` cannot be lazy since the value is known only when all emitters are either executed or discarded (due to signal combination). A statement such as `emit S(2)` is handled as `emit S; ?S:=2;` by the constructiveness test.

Advanced Constructiveness

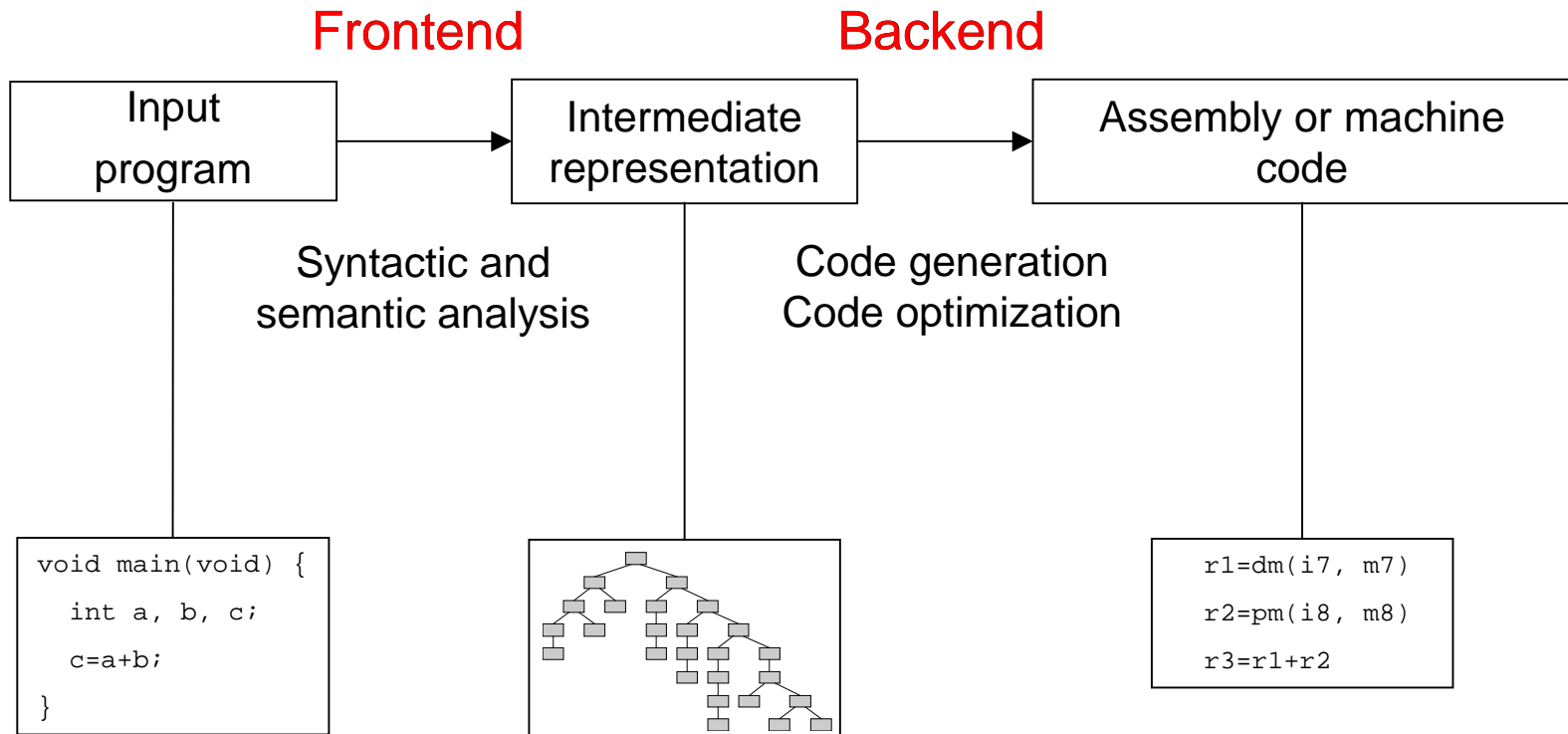
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A statement such as `emit S(2)` is handled as `emit S; ?S:=2;` by the constructiveness test.

Example

```
signal S1, S2 in
  present I then emit S1 else emit S2
||
  present S1 then
    call P1() ();
    emit S2
  end present
||
  present S2 then
    call P2() ();
    emit S1
  end present
end signal
```

constructive

Compiler Structure



Detailed Compiler Structure

